

**FACULTY OF ENGINEERING**  
**B.E. (M/P) VII-Semester (Main & Backlog) Examination, March/April 2021**

**Subject : Finite Element Analysis**

Time: 2 hours

Max. Marks: 70

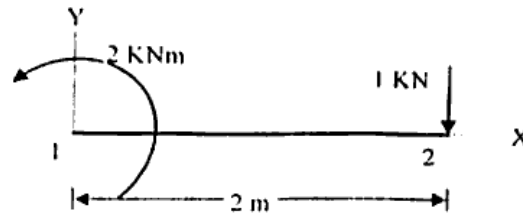
Note: Missing Data, if any, may be suitably be assumed.

**PART – A**

Answer any five questions.

(5x2 = 10 Marks)

- 1 What are the properties of stiffness matrix?
- 2 State the principle of minimum potential energy.
- 3 Write the stiffness matrix for plane frame element.
- 4 Determine the load vector for the beam element shown in figure.



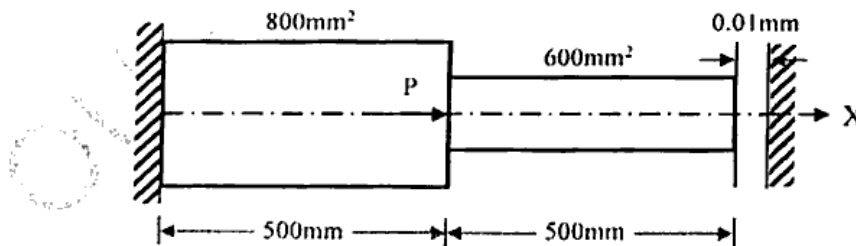
- 5 State strain – displacement relations for a plane strain problem.
- 6 In a plane stress problem,  $\sigma_x = 100$  MPa,  $\epsilon_y = 0.001$ ,  $E = 200$  GPa and  $\nu = 0.25$ . Determine the normal strain in z-direction ( $\epsilon_z$ ).
- 7 Differentiate between isoparametric and subparametric elements.
- 8 What is meant by isoparametric formulation?
- 9 What are the convergence requirements of finite element method?
- 10 What are the properties of eigen vectors?

**PART – B**

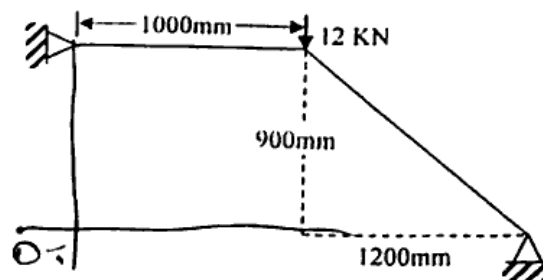
Answer any four questions.

(4x15=60 Marks)

- 11 For the stepped bar shown in figure 1, determine the nodal displacements and element stresses. Take  $E = 70$  GPa,  $P = 50$  kN,  $\alpha = 20 \times 10^{-6}/^\circ\text{C}$  and  $\Delta T = 50^\circ\text{C}$ .

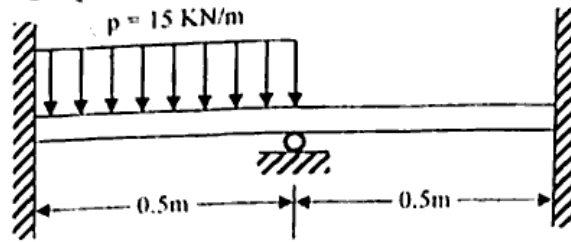


- 12 Find the nodal displacements and element stresses in the truss shown in figure 2. Take  $E = 200$  GPa,  $A = 600$  mm<sup>2</sup> for all members.

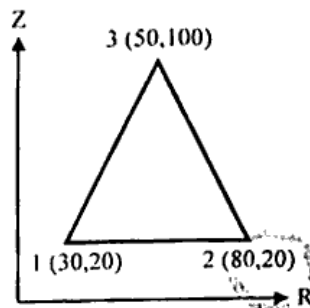


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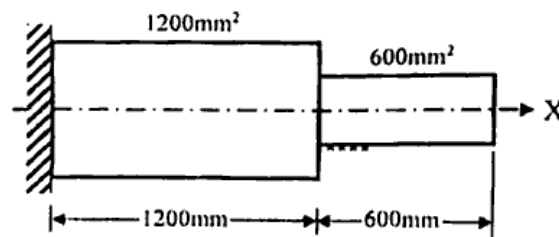
- 13 For the beam shown in figure 3, determine the deflection and slope if  $E = 200 \text{ GPa}$  and  $I = 5 \times 10^4 \text{ mm}^4$ .



- 14 (a) Derive the strain displacement matrix for a 3-noded triangular element.  
 (b) Determine the element stiffness matrix for the axisymmetric triangular element shown in figure 4. Take  $E = 210 \text{ GPa}$  and  $\nu = 0.25$ .



- 15 (a) Derive the shape functions for 4-noded quadrilateral element using natural coordinates.  
 (b) What is numerical integration? Explain in brief about Gauss quadrature method.  
 (c) What are global, local and natural coordinates?
- 16 Determine the temperature distribution in the circular fin of diameter 1 cm and length 8 cm. Base of the fin is maintained at  $100^\circ \text{ C}$  and convection takes place throughout the surface including the tip. The ambient temperature is  $20^\circ \text{ C}$ . Assuming the fin has two linear elements. Take  $k = 2 \text{ W/cm}^\circ \text{ C}$  and  $h = 0.2 \text{ W/cm}^2^\circ \text{ C}$ .
- 17 Determine the eigen values and eigen vectors for the stepped bar shown in figure 5. Take  $E = 200 \text{ GPa}$  and  $\rho = 7500 \text{ kg/m}^3$ .



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